

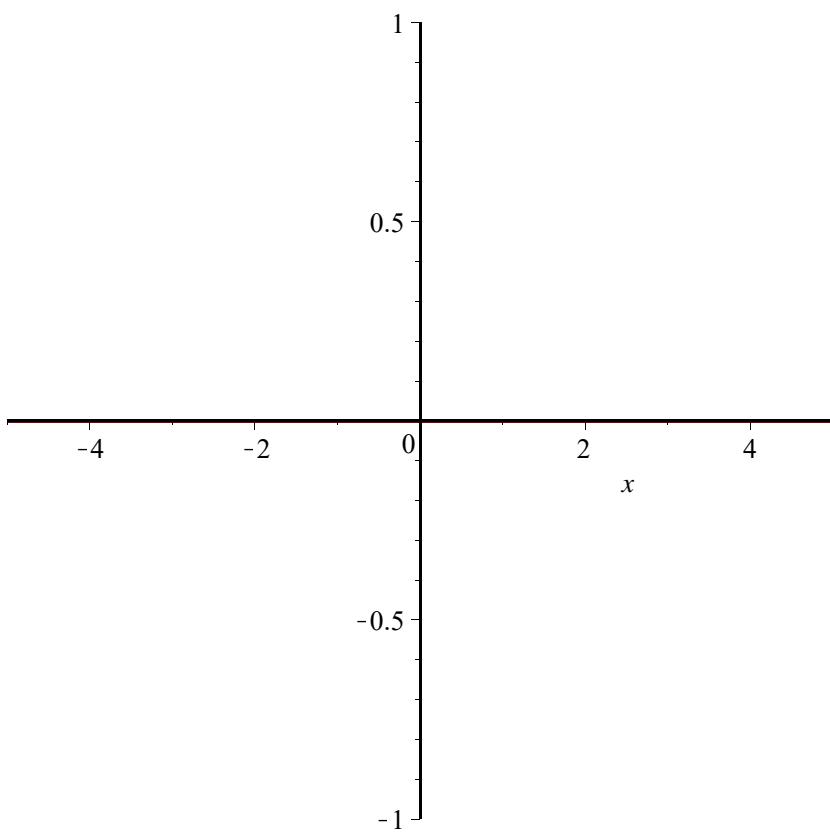
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> restart; G(s) :=  $\left( \cos\left(\frac{\text{Pi}}{2} \cdot s\right) \right)^2$ ; ui := piecewise(
    -1 < x - t < 1 and -1 < x + t < 1,
     $\frac{1}{2} \text{int}(G(s), s=x-t..x+t)$ , -1 < x - t < 1 and x + t > 1,  $\frac{1}{2} \text{int}(G(s), s=x-t..1)$ , x
    - t < -1 and -1 < x + t < 1,  $\frac{1}{2} \text{int}(G(s), s=-1..x+t)$ , x - t < -1 and x + t > 1,
     $\frac{1}{2} \text{int}(G(s), s=-1..1)$ , 0
)
G := s →  $\cos\left(\frac{1}{2} \pi s\right)^2$ 

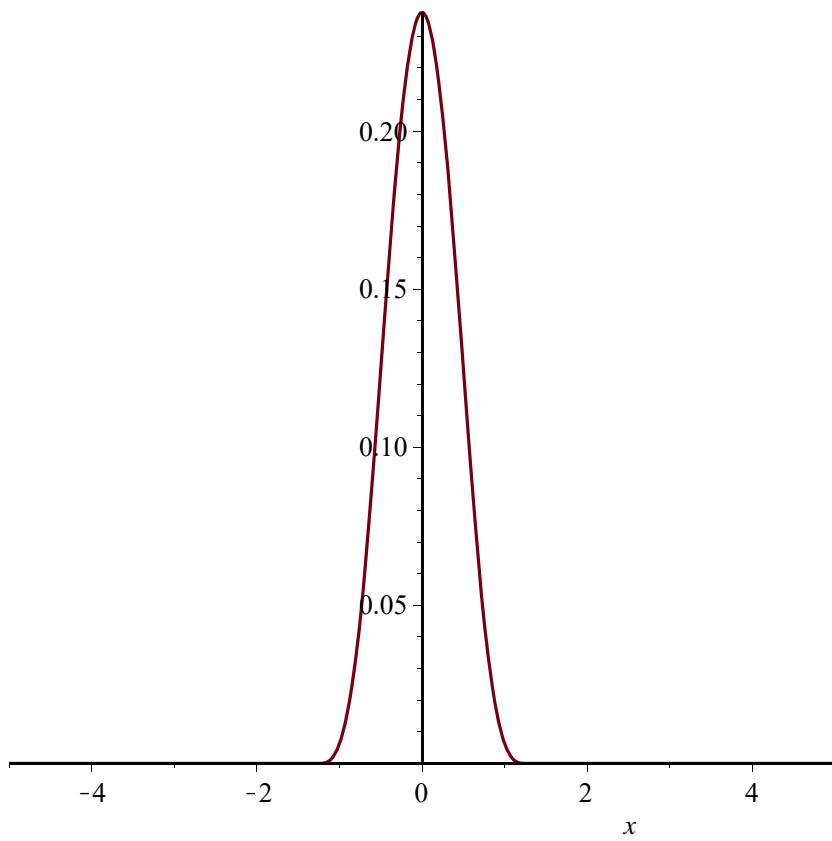
ui := 
$$\begin{cases} \frac{1}{2} \frac{\pi t + \cos\left(\frac{1}{2} \pi (-x+t)\right) \sin\left(\frac{1}{2} \pi (-x+t)\right) + \cos\left(\frac{1}{2} \pi (x+t)\right) \sin\left(\frac{1}{2} \pi (x+t)\right)}{\pi} & -1 < x \\ \frac{1}{4} \frac{\pi t - \pi x + 2 \cos\left(\frac{1}{2} \pi (-x+t)\right) \sin\left(\frac{1}{2} \pi (-x+t)\right) + \pi}{\pi} & \\ \frac{1}{4} \frac{\pi t + \pi x + 2 \cos\left(\frac{1}{2} \pi (x+t)\right) \sin\left(\frac{1}{2} \pi (x+t)\right) + \pi}{\pi} & \\ \frac{1}{2} & \\ 0 & \end{cases}$$


> for i from 0 to 5 by 0.25 do u1 := subs(t=i, ui) : plot(u1, x=-5..5) end do
u1 := 
$$\begin{cases} \frac{1}{2} \frac{\cos\left(-\frac{1}{2} \pi x\right) \sin\left(-\frac{1}{2} \pi x\right) + \cos\left(\frac{1}{2} \pi x\right) \sin\left(\frac{1}{2} \pi x\right)}{\pi} & -1 < x \text{ and } x < 1 \\ \frac{1}{4} \frac{-\pi x + 2 \cos\left(-\frac{1}{2} \pi x\right) \sin\left(-\frac{1}{2} \pi x\right) + \pi}{\pi} & -1 < x \text{ and } x < 1 \text{ and } 1 < x \\ \frac{1}{4} \frac{\pi x + 2 \cos\left(\frac{1}{2} \pi x\right) \sin\left(\frac{1}{2} \pi x\right) + \pi}{\pi} & x < -1 \text{ and } -1 < x \text{ and } x < 1 \\ \frac{1}{2} & x < -1 \text{ and } 1 < x \\ 0 & otherwise \end{cases}$$

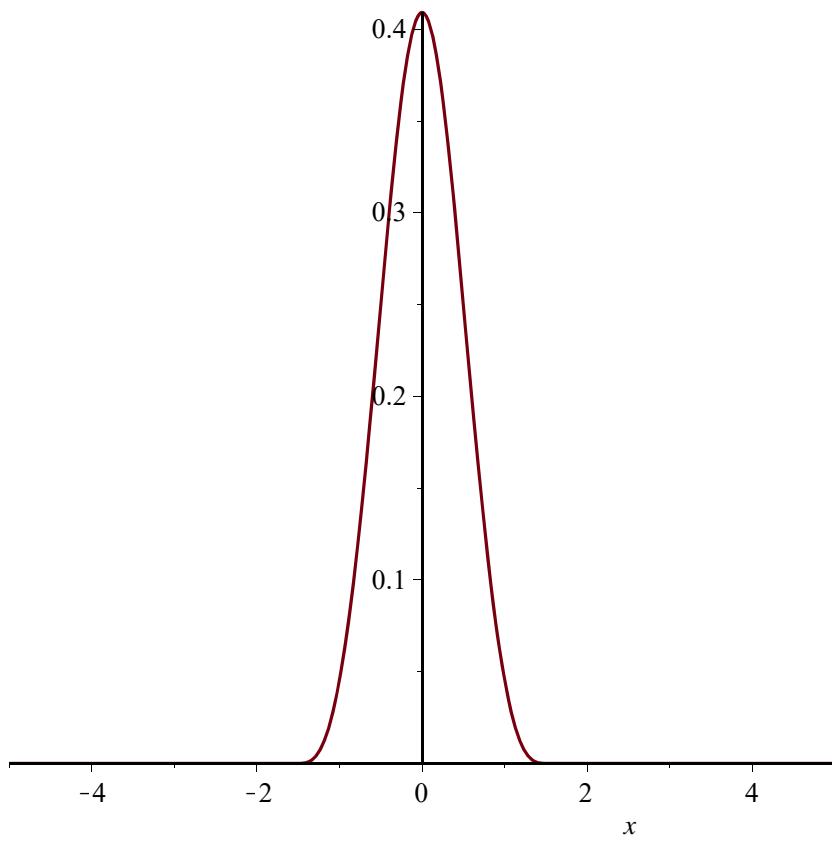

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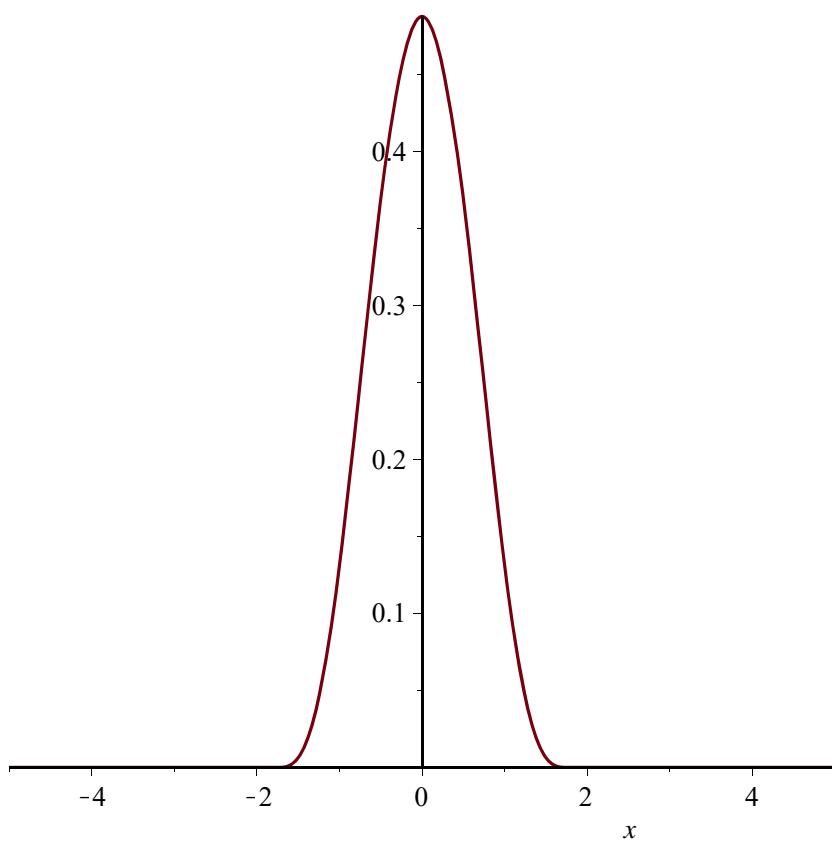
$$u_I := \begin{cases} \frac{1}{2} \frac{0.25\pi + \cos\left(\frac{1}{2}\pi(-x+0.25)\right)\sin\left(\frac{1}{2}\pi(-x+0.25)\right) + \cos\left(\frac{1}{2}\pi(x+0.25)\right)\sin\left(\frac{1}{2}\pi(x+0.25)\right)}{\pi} & x < -2 \\ \frac{1}{4} \frac{1.25\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(-x+0.25)\right)\sin\left(\frac{1}{2}\pi(-x+0.25)\right)}{\pi} & -2 \leq x < 0 \\ \frac{1}{4} \frac{1.25\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+0.25)\right)\sin\left(\frac{1}{2}\pi(x+0.25)\right)}{\pi} & 0 < x < 2 \\ \frac{1}{2} & x = 2 \\ 0 & x > 2 \end{cases}$$



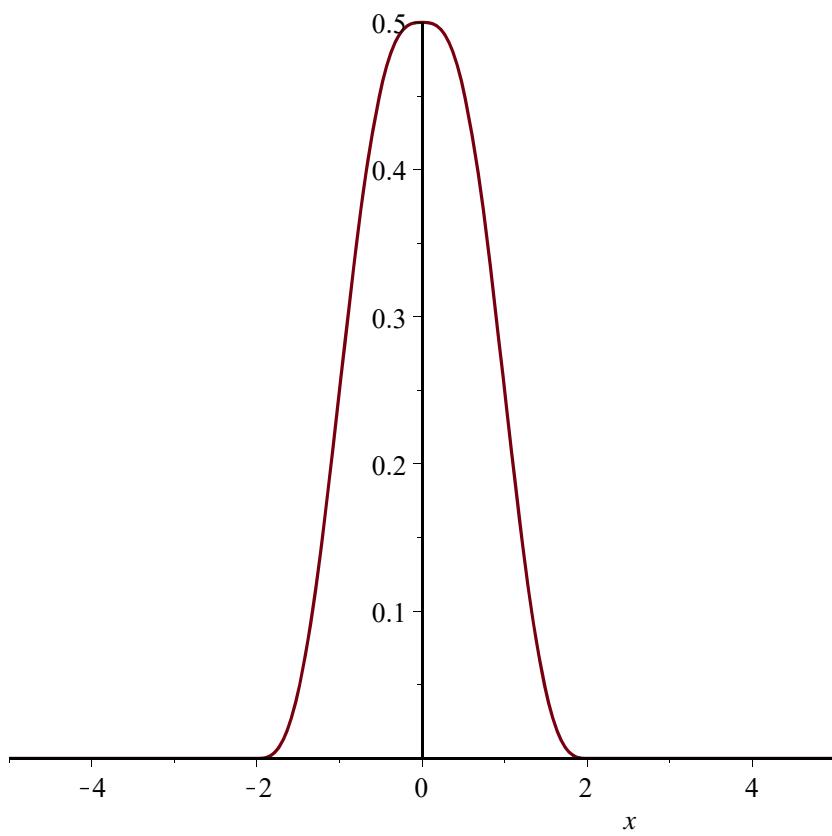
$$uI := \begin{cases} \frac{1}{2} \frac{0.50\pi + \cos\left(\frac{1}{2}\pi(-x+0.50)\right) \sin\left(\frac{1}{2}\pi(-x+0.50)\right) + \cos\left(\frac{1}{2}\pi(x+0.50)\right) \sin\left(\frac{1}{2}\pi(x+0.50)\right)}{\pi} \\ \frac{1}{4} \frac{1.50\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(-x+0.50)\right) \sin\left(\frac{1}{2}\pi(-x+0.50)\right)}{\pi} \\ \frac{1}{4} \frac{1.50\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+0.50)\right) \sin\left(\frac{1}{2}\pi(x+0.50)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



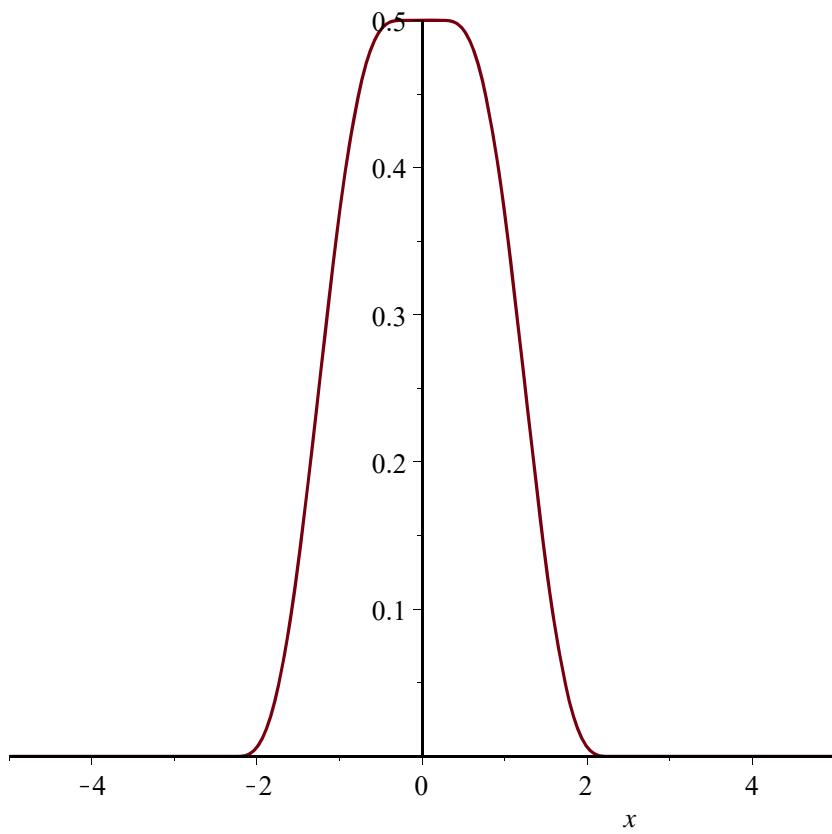
$$uI := \begin{cases} \frac{1}{2} \frac{0.75\pi + \cos\left(\frac{1}{2}\pi(0.75-x)\right)\sin\left(\frac{1}{2}\pi(0.75-x)\right) + \cos\left(\frac{1}{2}\pi(x+0.75)\right)\sin\left(\frac{1}{2}\pi(x+0.75)\right)}{\pi} \\ \frac{1}{4} \frac{1.75\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(0.75-x)\right)\sin\left(\frac{1}{2}\pi(0.75-x)\right)}{\pi} \\ \frac{1}{4} \frac{1.75\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+0.75)\right)\sin\left(\frac{1}{2}\pi(x+0.75)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



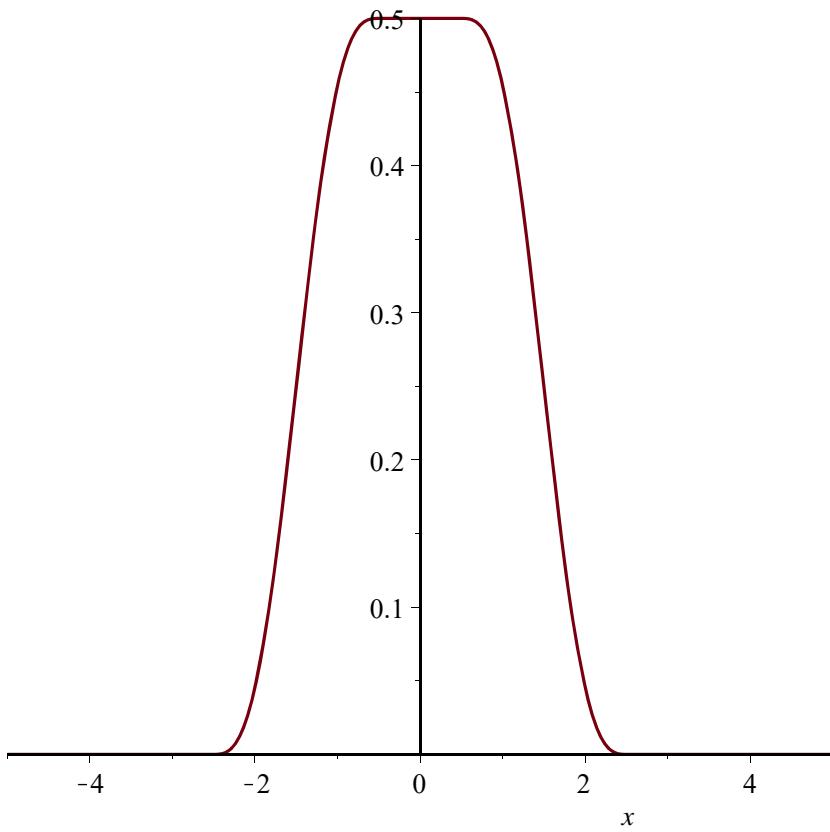
$$uI := \begin{cases} \frac{1}{2} \frac{1.00\pi + \cos\left(\frac{1}{2}\pi(-x+1.00)\right)\sin\left(\frac{1}{2}\pi(-x+1.00)\right) + \cos\left(\frac{1}{2}\pi(x+1.00)\right)\sin\left(\frac{1}{2}\pi(x+1.00)\right)}{\pi} \\ \frac{1}{4} \frac{2.00\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(-x+1.00)\right)\sin\left(\frac{1}{2}\pi(-x+1.00)\right)}{\pi} \\ \frac{1}{4} \frac{2.00\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+1.00)\right)\sin\left(\frac{1}{2}\pi(x+1.00)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



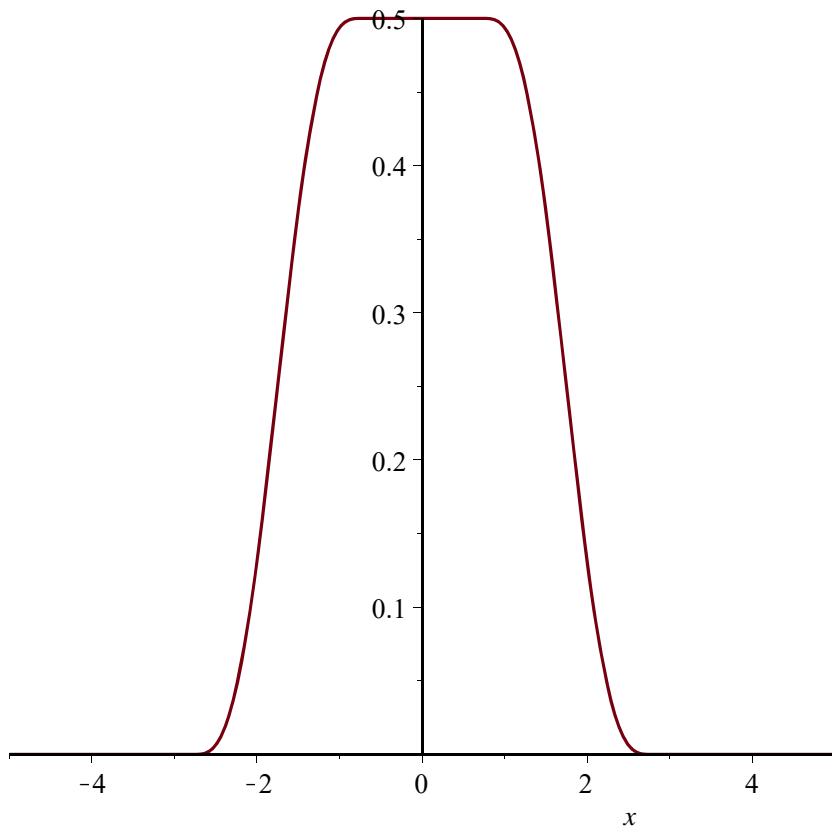
$$uI := \begin{cases} \frac{1}{2} \frac{1.25\pi + \cos\left(\frac{1}{2}\pi(1.25-x)\right)\sin\left(\frac{1}{2}\pi(1.25-x)\right) + \cos\left(\frac{1}{2}\pi(x+1.25)\right)\sin\left(\frac{1}{2}\pi(x+1.25)\right)}{\pi} \\ \frac{1}{4} \frac{2.25\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(1.25-x)\right)\sin\left(\frac{1}{2}\pi(1.25-x)\right)}{\pi} \\ \frac{1}{4} \frac{2.25\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+1.25)\right)\sin\left(\frac{1}{2}\pi(x+1.25)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



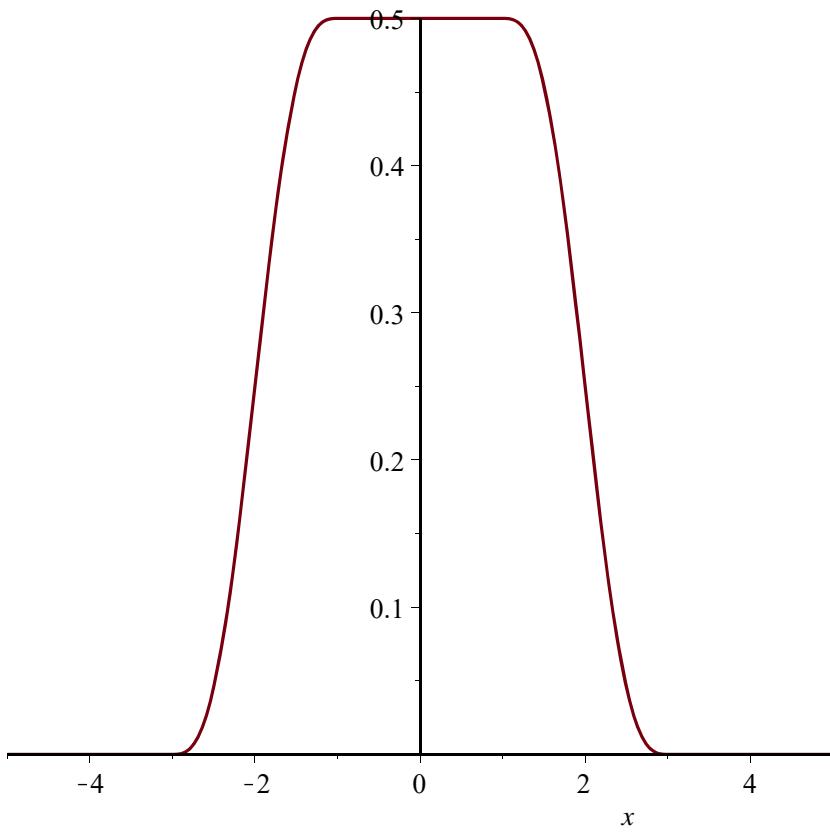
$$uI := \begin{cases} \frac{1}{2} \frac{1.50\pi + \cos\left(\frac{1}{2}\pi(1.50-x)\right)\sin\left(\frac{1}{2}\pi(1.50-x)\right) + \cos\left(\frac{1}{2}\pi(x+1.50)\right)\sin\left(\frac{1}{2}\pi(x+1.50)\right)}{\pi} \\ \frac{1}{4} \frac{2.50\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(1.50-x)\right)\sin\left(\frac{1}{2}\pi(1.50-x)\right)}{\pi} \\ \frac{1}{4} \frac{2.50\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+1.50)\right)\sin\left(\frac{1}{2}\pi(x+1.50)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



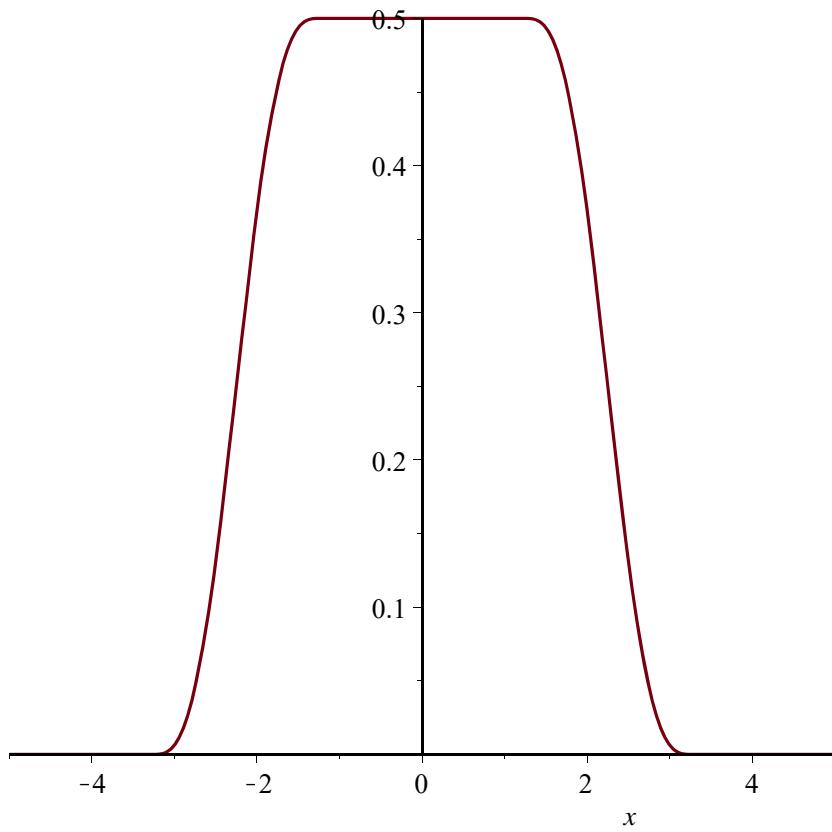
$$uI := \begin{cases} \frac{1}{2} \frac{1.75\pi + \cos\left(\frac{1}{2}\pi(1.75-x)\right) \sin\left(\frac{1}{2}\pi(1.75-x)\right) + \cos\left(\frac{1}{2}\pi(x+1.75)\right) \sin\left(\frac{1}{2}\pi(x+1.75)\right)}{\pi} \\ \frac{1}{4} \frac{2.75\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(1.75-x)\right) \sin\left(\frac{1}{2}\pi(1.75-x)\right)}{\pi} \\ \frac{1}{4} \frac{2.75\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+1.75)\right) \sin\left(\frac{1}{2}\pi(x+1.75)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



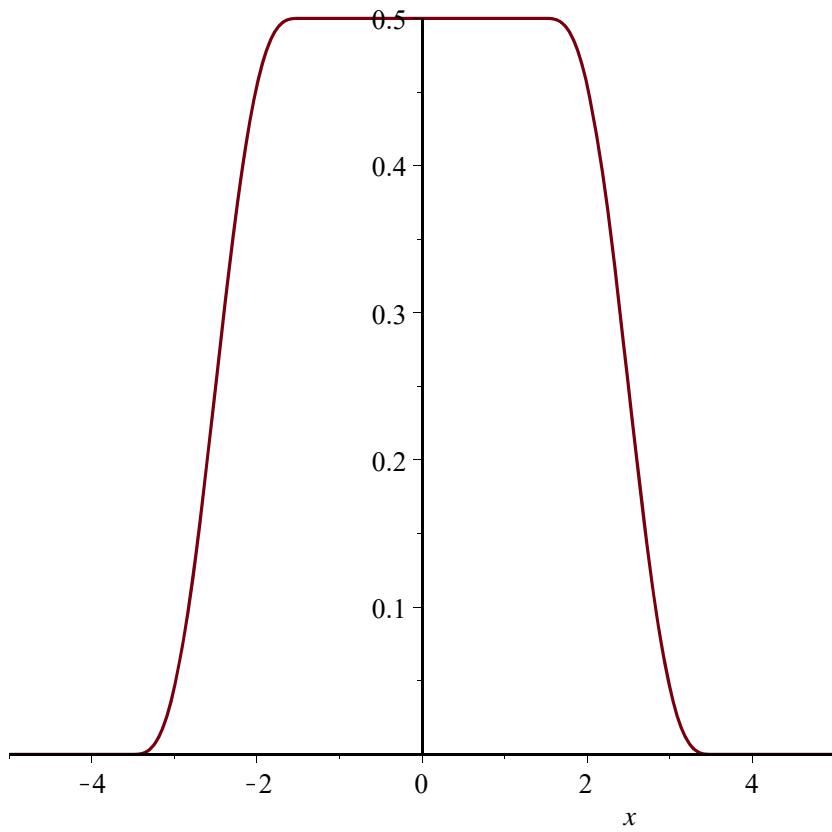
$$uI := \begin{cases} \frac{1}{2} \frac{2.00\pi + \cos\left(\frac{1}{2}\pi(2.00-x)\right)\sin\left(\frac{1}{2}\pi(2.00-x)\right) + \cos\left(\frac{1}{2}\pi(x+2.00)\right)\sin\left(\frac{1}{2}\pi(x+2.00)\right)}{\pi} \\ \frac{1}{4} \frac{3.00\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(2.00-x)\right)\sin\left(\frac{1}{2}\pi(2.00-x)\right)}{\pi} \\ \frac{1}{4} \frac{3.00\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+2.00)\right)\sin\left(\frac{1}{2}\pi(x+2.00)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



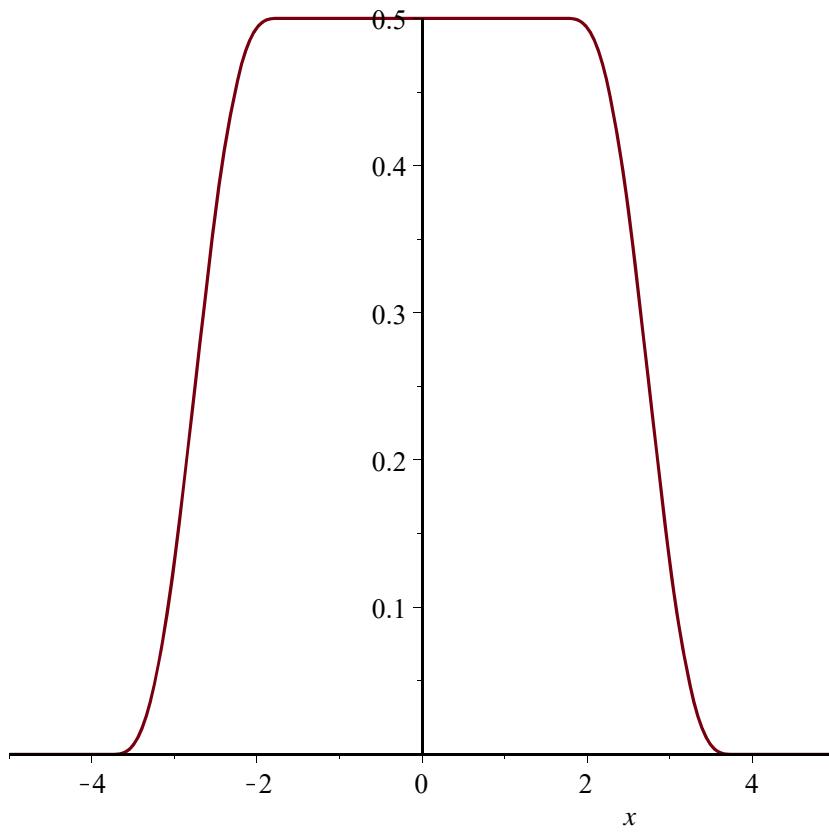
$$uI := \begin{cases} \frac{1}{2} \frac{2.25\pi + \cos\left(\frac{1}{2}\pi(2.25-x)\right)\sin\left(\frac{1}{2}\pi(2.25-x)\right) + \cos\left(\frac{1}{2}\pi(x+2.25)\right)\sin\left(\frac{1}{2}\pi(x+2.25)\right)}{\pi} \\ \frac{1}{4} \frac{3.25\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(2.25-x)\right)\sin\left(\frac{1}{2}\pi(2.25-x)\right)}{\pi} \\ \frac{1}{4} \frac{3.25\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+2.25)\right)\sin\left(\frac{1}{2}\pi(x+2.25)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



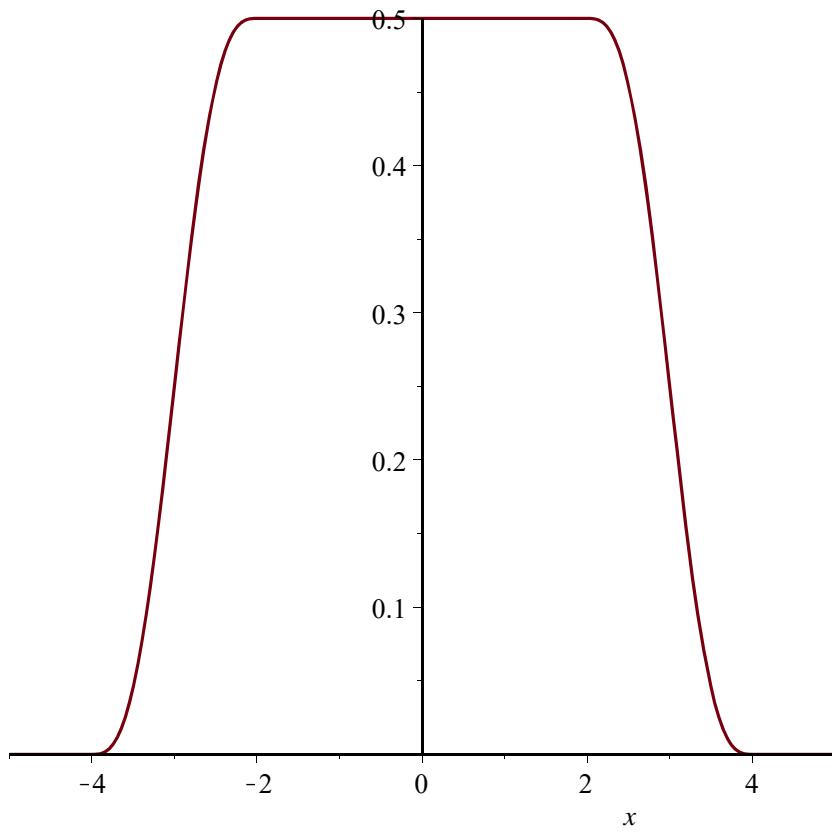
$$uI := \begin{cases} \frac{1}{2} \frac{2.50\pi + \cos\left(\frac{1}{2}\pi(2.50-x)\right)\sin\left(\frac{1}{2}\pi(2.50-x)\right) + \cos\left(\frac{1}{2}\pi(x+2.50)\right)\sin\left(\frac{1}{2}\pi(x+2.50)\right)}{\pi} \\ \frac{1}{4} \frac{3.50\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(2.50-x)\right)\sin\left(\frac{1}{2}\pi(2.50-x)\right)}{\pi} \\ \frac{1}{4} \frac{3.50\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+2.50)\right)\sin\left(\frac{1}{2}\pi(x+2.50)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



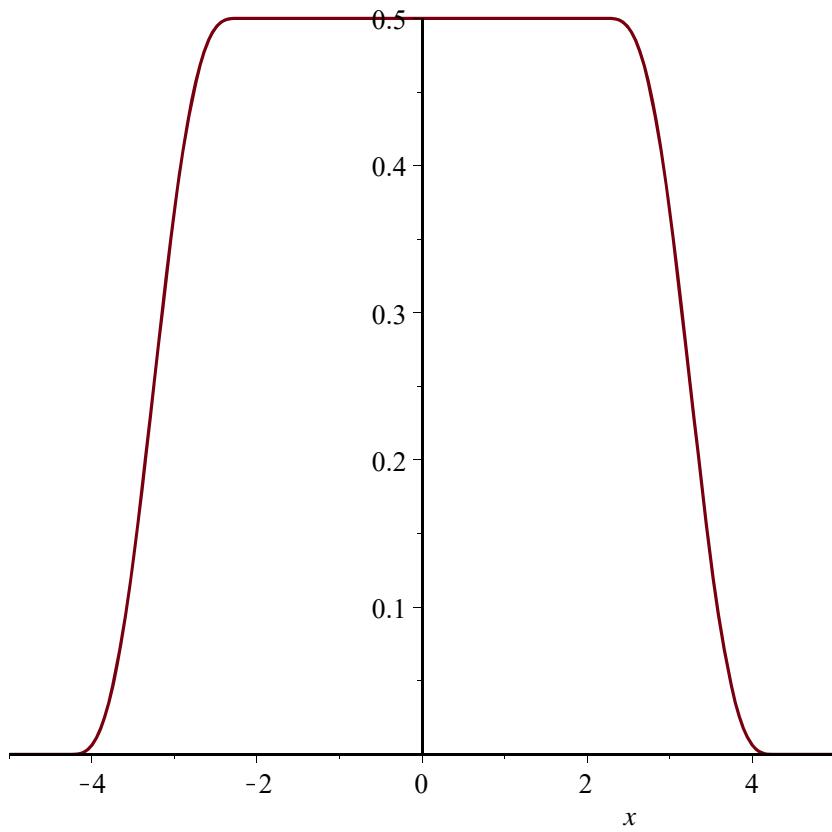
$$uI := \begin{cases} \frac{1}{2} \frac{2.75\pi + \cos\left(\frac{1}{2}\pi(2.75-x)\right)\sin\left(\frac{1}{2}\pi(2.75-x)\right) + \cos\left(\frac{1}{2}\pi(x+2.75)\right)\sin\left(\frac{1}{2}\pi(x+2.75)\right)}{\pi} \\ \frac{1}{4} \frac{3.75\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(2.75-x)\right)\sin\left(\frac{1}{2}\pi(2.75-x)\right)}{\pi} \\ \frac{1}{4} \frac{3.75\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+2.75)\right)\sin\left(\frac{1}{2}\pi(x+2.75)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



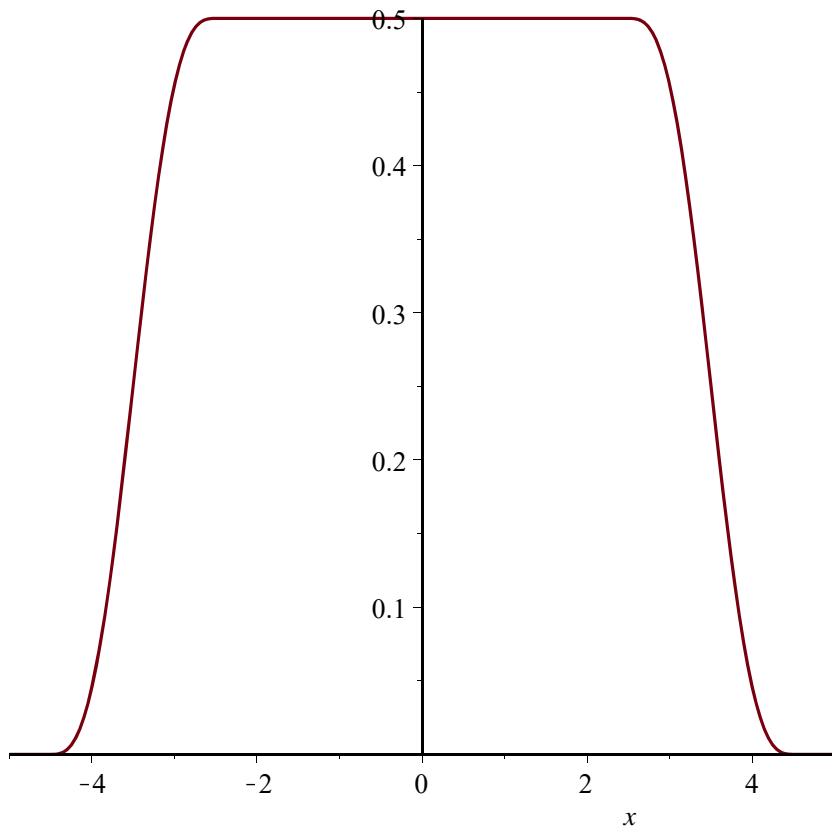
$$uI := \begin{cases} \frac{1}{2} \frac{3.00\pi + \cos\left(\frac{1}{2}\pi(3.00-x)\right)\sin\left(\frac{1}{2}\pi(3.00-x)\right) + \cos\left(\frac{1}{2}\pi(x+3.00)\right)\sin\left(\frac{1}{2}\pi(x+3.00)\right)}{\pi} \\ \frac{1}{4} \frac{4.00\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(3.00-x)\right)\sin\left(\frac{1}{2}\pi(3.00-x)\right)}{\pi} \\ \frac{1}{4} \frac{4.00\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+3.00)\right)\sin\left(\frac{1}{2}\pi(x+3.00)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



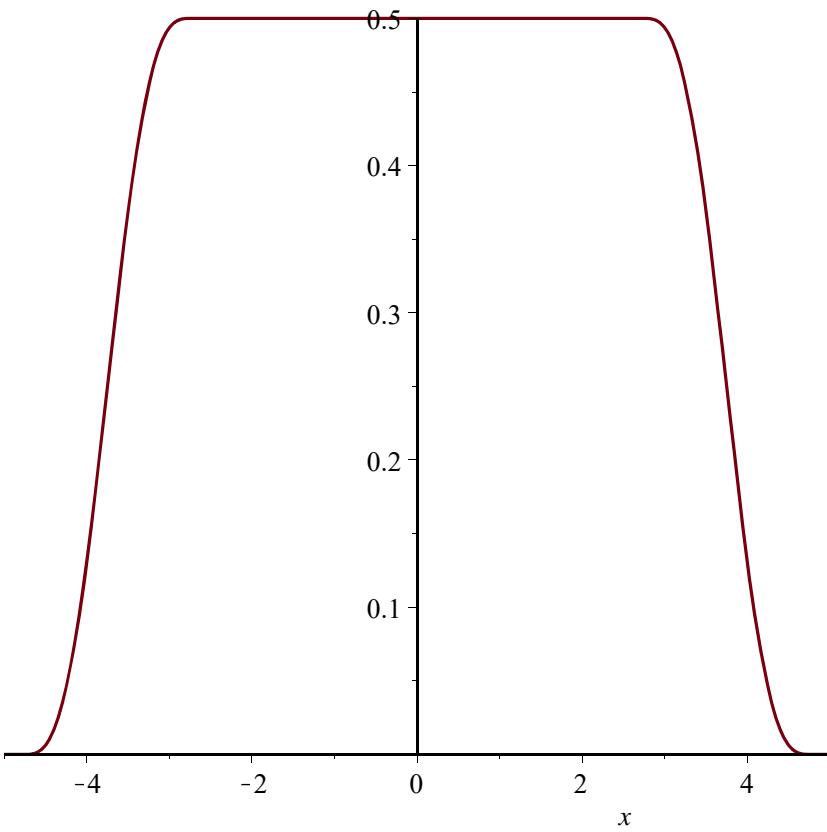
$$uI := \begin{cases} \frac{1}{2} \frac{3.25\pi + \cos\left(\frac{1}{2}\pi(3.25-x)\right)\sin\left(\frac{1}{2}\pi(3.25-x)\right) + \cos\left(\frac{1}{2}\pi(x+3.25)\right)\sin\left(\frac{1}{2}\pi(x+3.25)\right)}{\pi} & -3.25 \leq x < -2.5 \\ \frac{1}{4} \frac{4.25\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(3.25-x)\right)\sin\left(\frac{1}{2}\pi(3.25-x)\right)}{\pi} & -2.5 \leq x < 2.5 \\ \frac{1}{4} \frac{4.25\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+3.25)\right)\sin\left(\frac{1}{2}\pi(x+3.25)\right)}{\pi} & 2.5 \leq x < 3.25 \\ \frac{1}{2} & 3.25 \leq x < 4 \\ 0 & x \geq 4 \end{cases}$$



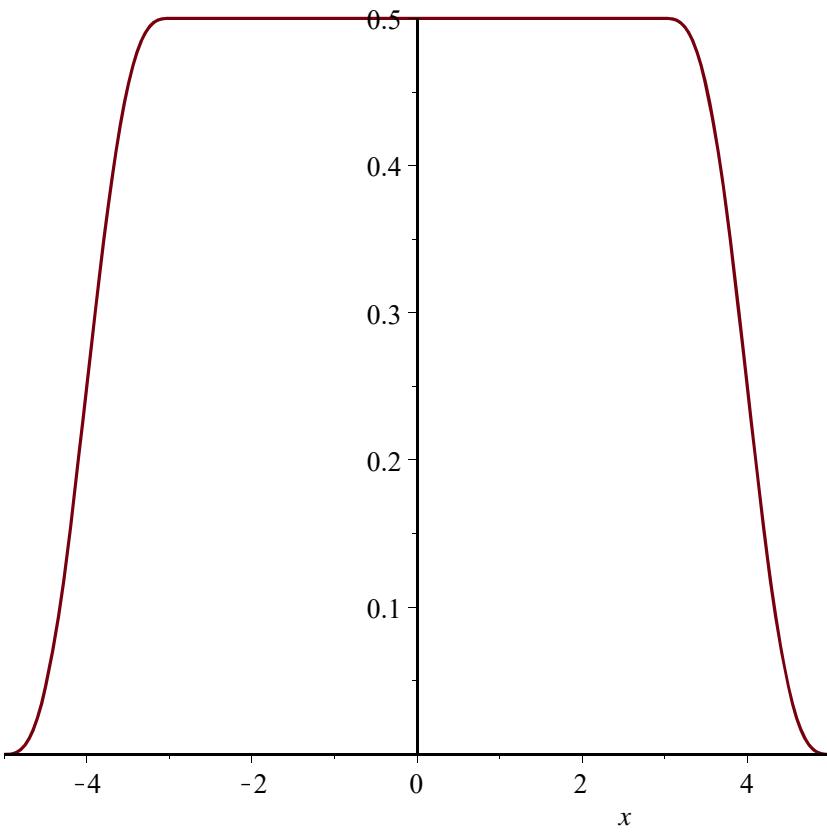
$$uI := \begin{cases} \frac{1}{2} \frac{3.50\pi + \cos\left(\frac{1}{2}\pi(3.50-x)\right)\sin\left(\frac{1}{2}\pi(3.50-x)\right) + \cos\left(\frac{1}{2}\pi(x+3.50)\right)\sin\left(\frac{1}{2}\pi(x+3.50)\right)}{\pi} \\ \frac{1}{4} \frac{4.50\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(3.50-x)\right)\sin\left(\frac{1}{2}\pi(3.50-x)\right)}{\pi} \\ \frac{1}{4} \frac{4.50\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+3.50)\right)\sin\left(\frac{1}{2}\pi(x+3.50)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



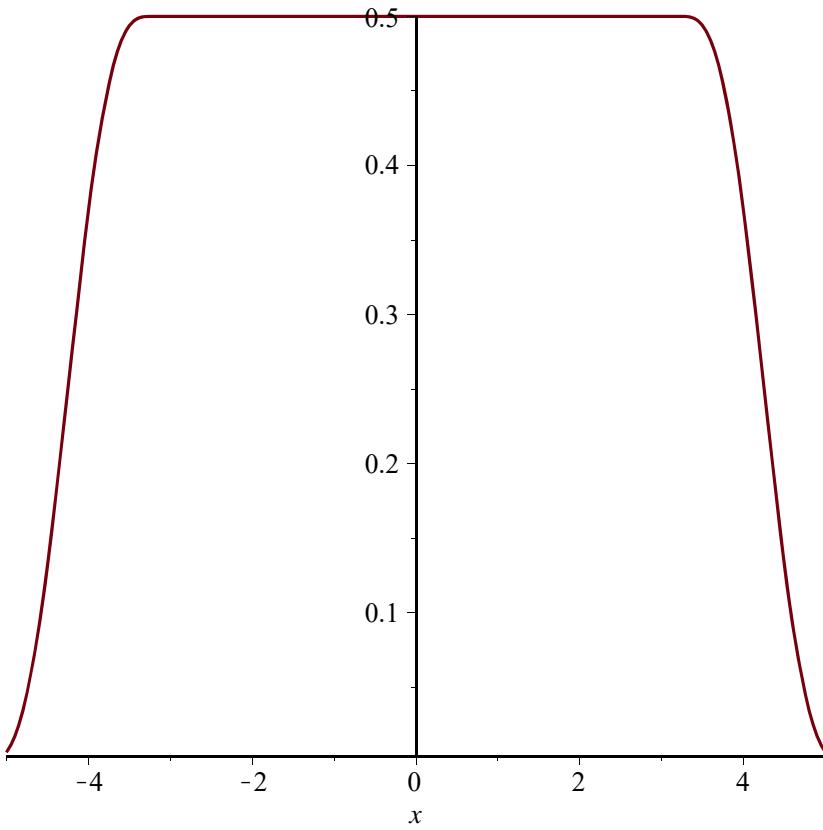
$$uI := \begin{cases} \frac{1}{2} \frac{3.75\pi + \cos\left(\frac{1}{2}\pi(3.75-x)\right)\sin\left(\frac{1}{2}\pi(3.75-x)\right) + \cos\left(\frac{1}{2}\pi(x+3.75)\right)\sin\left(\frac{1}{2}\pi(x+3.75)\right)}{\pi} \\ \frac{1}{4} \frac{4.75\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(3.75-x)\right)\sin\left(\frac{1}{2}\pi(3.75-x)\right)}{\pi} \\ \frac{1}{4} \frac{4.75\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+3.75)\right)\sin\left(\frac{1}{2}\pi(x+3.75)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



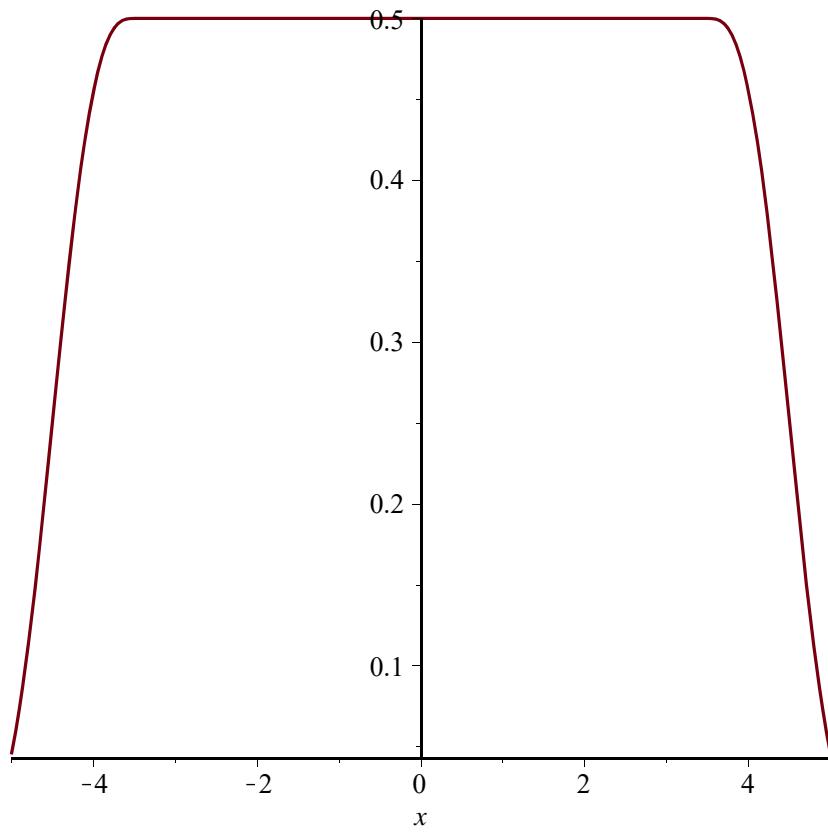
$$uI := \begin{cases} \frac{1}{2} \frac{4.00\pi + \cos\left(\frac{1}{2}\pi(4.00-x)\right)\sin\left(\frac{1}{2}\pi(4.00-x)\right) + \cos\left(\frac{1}{2}\pi(x+4.00)\right)\sin\left(\frac{1}{2}\pi(x+4.00)\right)}{\pi} \\ \frac{1}{4} \frac{5.00\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(4.00-x)\right)\sin\left(\frac{1}{2}\pi(4.00-x)\right)}{\pi} \\ \frac{1}{4} \frac{5.00\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+4.00)\right)\sin\left(\frac{1}{2}\pi(x+4.00)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



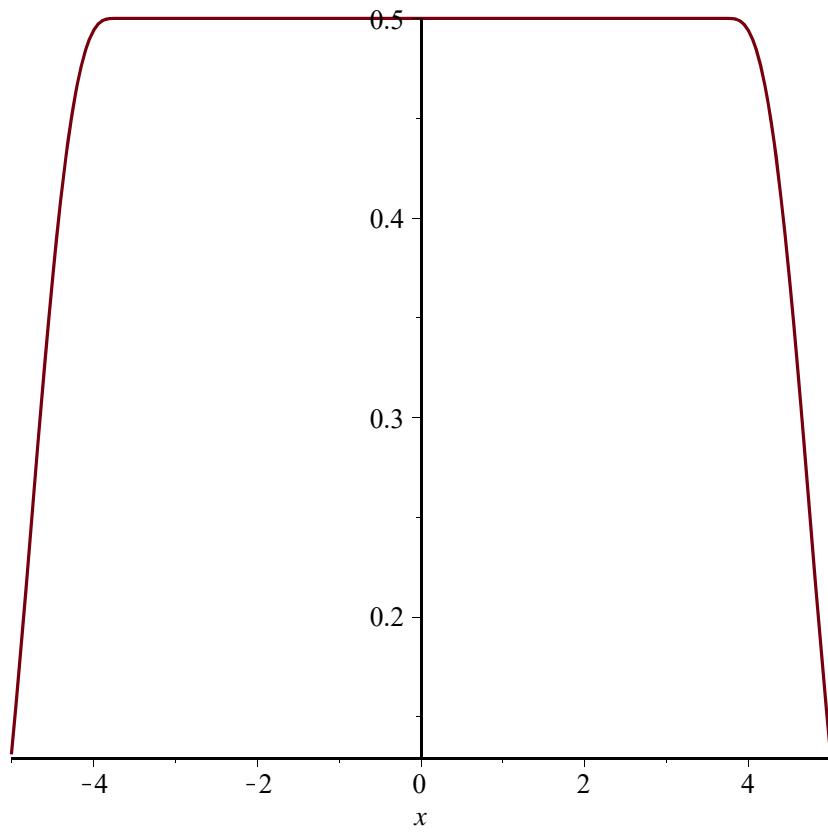
$$uI := \begin{cases} \frac{1}{2} \frac{4.25\pi + \cos\left(\frac{1}{2}\pi(4.25-x)\right)\sin\left(\frac{1}{2}\pi(4.25-x)\right) + \cos\left(\frac{1}{2}\pi(x+4.25)\right)\sin\left(\frac{1}{2}\pi(x+4.25)\right)}{\pi} \\ \frac{1}{4} \frac{5.25\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(4.25-x)\right)\sin\left(\frac{1}{2}\pi(4.25-x)\right)}{\pi} \\ \frac{1}{4} \frac{5.25\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+4.25)\right)\sin\left(\frac{1}{2}\pi(x+4.25)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



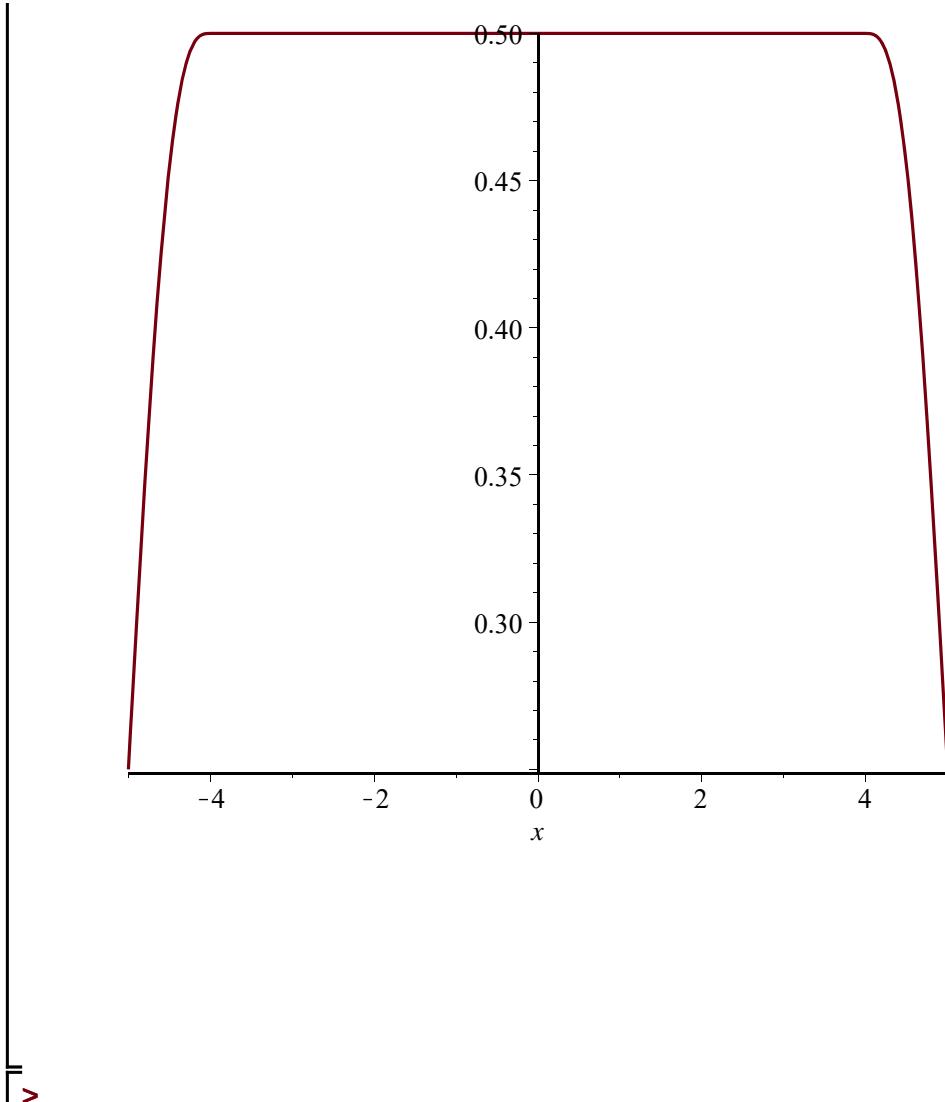
$$uI := \begin{cases} \frac{1}{2} \frac{4.50\pi + \cos\left(\frac{1}{2}\pi(4.50-x)\right)\sin\left(\frac{1}{2}\pi(4.50-x)\right) + \cos\left(\frac{1}{2}\pi(x+4.50)\right)\sin\left(\frac{1}{2}\pi(x+4.50)\right)}{\pi} \\ \frac{1}{4} \frac{5.50\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(4.50-x)\right)\sin\left(\frac{1}{2}\pi(4.50-x)\right)}{\pi} \\ \frac{1}{4} \frac{5.50\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+4.50)\right)\sin\left(\frac{1}{2}\pi(x+4.50)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



$$uI := \begin{cases} \frac{1}{2} \frac{4.75\pi + \cos\left(\frac{1}{2}\pi(4.75-x)\right)\sin\left(\frac{1}{2}\pi(4.75-x)\right) + \cos\left(\frac{1}{2}\pi(x+4.75)\right)\sin\left(\frac{1}{2}\pi(x+4.75)\right)}{\pi} \\ \frac{1}{4} \frac{5.75\pi - \pi x + 2\cos\left(\frac{1}{2}\pi(4.75-x)\right)\sin\left(\frac{1}{2}\pi(4.75-x)\right)}{\pi} \\ \frac{1}{4} \frac{5.75\pi + \pi x + 2\cos\left(\frac{1}{2}\pi(x+4.75)\right)\sin\left(\frac{1}{2}\pi(x+4.75)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



$$uI := \begin{cases} \frac{1}{2} \frac{5.00 \pi + \cos\left(\frac{1}{2} \pi (5.00 - x)\right) \sin\left(\frac{1}{2} \pi (5.00 - x)\right) + \cos\left(\frac{1}{2} \pi (x + 5.00)\right) \sin\left(\frac{1}{2} \pi (x + 5.00)\right)}{\pi} \\ \frac{1}{4} \frac{6.00 \pi - \pi x + 2 \cos\left(\frac{1}{2} \pi (5.00 - x)\right) \sin\left(\frac{1}{2} \pi (5.00 - x)\right)}{\pi} \\ \frac{1}{4} \frac{6.00 \pi + \pi x + 2 \cos\left(\frac{1}{2} \pi (x + 5.00)\right) \sin\left(\frac{1}{2} \pi (x + 5.00)\right)}{\pi} \\ \frac{1}{2} \\ 0 \end{cases}$$



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